

Package: HMMRel (via r-universe)

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Title Hidden Markov Models for Reliability and Maintenance

Version 0.1.1

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Description Reliability Analysis and Maintenance Optimization using Hidden Markov Models (HMM). The use of HMMs to model the state of a system which is not directly observable and instead certain indicators (signals) of the true situation are provided via a control system. A hidden model can provide key information about the system dependability, such as the reliability of the system and related measures. An estimation procedure is implemented based on the Baum-Welch algorithm. Classical structures such as K-out-of-N systems and Shock models are illustrated. Finally, the maintenance of the system is considered in the HMM context and two functions for new preventive maintenance strategies are considered. Maintenance efficiency is measured in terms of expected cost. Methods are described in Gamiz, Limnios, and Segovia-Garcia (2023) <[doi:10.1016/j.ejor.2022.05.006](https://doi.org/10.1016/j.ejor.2022.05.006)>.

License GPL-2

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HMMRel-package	<i>HMMRel - Hidden Markov Models for Reliability and Maintenance</i>
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Description

Reliability Analysis and Maintenance Optimization using Hidden Markov Models (HMM).

Details

Package: HMMRel
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Date: 2024-11-11
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Author(s)

M.L. Gamiz, N.Limnios, and M.C. Segovia-Garcia

References

Gamiz, M.L., Limnios, N., Segovia-Garcia, M.C. (2023). Hidden Markov models in reliability and maintenance. *European Journal of Operational Research*, 304(3), 1242-1255.

cost.cspc

*Maintenance Policy based on Critical State Probability Criteria.***Description**

Preventive maintenance based on Critical State Probability Criteria (CSPC).

Usage

```
cost.cspc(prob, hmmR, n.up1, cost.C, cost.P, t.max)
```

Arguments

prob	A real number in the interval (0,1).
hmmR	A hidden Markov Model.
n.up1	An integer value for indicating the total number of optimal performance states of the hidden MC.
cost.C	A positive real number denoting the cost value in monetary units incurred by a corrective maintenance action.
cost.P	A positive real number denoting the cost value in monetary units incurred by a preventive maintenance action.
t.max	A time value for the maximum time the system will be in use. After that time the system will not operate anymore.

Details

Preventive maintenance policies based on critical states probability criteria (CSPC) are considered. Roughly speaking, a preventive maintenance action is carried out once the system enters a subset of operational states that are considered critical in some sense. The subset of operative states up is in turn split into two subsets: optimal states or $up1$ and operative but critical states or $up2$, where $up=up1 \cup up2$. For a given probability value (prob) this function first calculates the optimal inspection time

$$t.insp = \min\{t > 0 : \Pr(X(t) \in up2, X(u) \in up1, \forall u < t) \geq prob\}.$$

The system is inspected every $t.insp$ time-units. At the time of inspection, any of three situations can be found:

1. the system is in failure, then the system is returned to operational conditions ($up1$), and a cost of $cost.C$ monetary-units is implied;
2. the system is in a state of $up2$, then a preventive maintenance action is carried out, returning the system to a state in $up1$ and implying a cost of $cost.P$ monetary-units; and
3. the system is found in a state of $up1$, then no maintenance action is carried out and there is no associated cost.

Value

time.insp	The time at which preventive maintenance is carried out.
t.max	The maximum time that the system is being used.
n.insp	The total number of inspections that are carried out during the system lifetime, i.e. in the interval (0, t.max).
total.cost	The total cost incurred by all maintenance actions (corrective and preventive) developed in the system.

Author(s)

M.L. Gamiz, N. Limnios, and M.C. Segovia-Garcia (2024)

References

Gamiz, M.L., Limnios, N., and Segovia-Garcia, M.C. (2023). Hidden Markov models in reliability and maintenance. *European Journal of Operational Research*, 304(3), 1242-1255.

See Also

See `cost.wspc` for the implementation of the WSPC algorithm for maintenance policy.

Examples

```

model<- 'other'
rate<-p<-NA
P<-matrix(c(8,2,1,0,6,4,6,2,2)/10,3,3,byrow=TRUE)
M<-matrix(c(7,3,0,4,3,3,0,4,6)/10,3,3,byrow=TRUE)
Nx<-3; Ny<-3
n.up<-2; n.green<-2
alpha<-c(1,0,0)
hmm1<-def.hmmR(model=model,rate=NA,p=NA,alpha=alpha,P=P,M=M,Nx=Nx,Ny=Ny,n.up=n.up,n.green=n.green)
prob<-0.8;
n.up1<-n.green1<-1;cost.C<-10;cost.P<-1;t.max<-50
cost1<-cost.cspc(prob=prob,hmmR=hmm1,n.up1=n.up1,cost.C=cost.C,cost.P=cost.P,t.max=t.max)
cost1
#
v.prob<-seq(0.1,0.99,length=100)
v.cost1<-inspection.time<-double(100)
for(i in 1:100)
{cost<-cost.cspc(prob=v.prob[i],hmmR=hmm1,n.up1=n.up1,
  cost.C=cost.C,cost.P=cost.P,t.max=t.max)
  v.cost1[i]<-cost$total.cost
  inspection.time[i]<-cost$time.insp
}
oldpar <- par(mar = c(5, 5, 10, 10))
plot(v.prob,v.cost1,type='s',main='CSPC Algorithm for Maintenance Policy',
  xlab='Probability of critical state',
  ylab='Cost of maintenance')
grid()
par(oldpar)

```

cost.wcspc

*Maintenance Policy based on Warning Signal Probability Criteria.***Description**

Preventive maintenance based on Warning Signal Probability Criteria (WSPC).

Usage

```
cost.wcspc(prob, hmmR, n.up1, n.green1, cost.C, cost.P, t.max)
```

Arguments

prob	A real number in the interval (0,1).
hmmR	A hidden Markov Model.
n.up1	An integer value for indicating the total number of optimal performance states of the hidden MC.
n.green1	An integer value for indicating the total number of safe signals. A safe signal indicates an optimal system performance.
cost.C	A positive real number denoting the cost value in monetary units incurred by a corrective maintenance action.
cost.P	A positive real number denoting the cost value in monetary units incurred by a preventive maintenance action.
t.max	A time value for the maximum time the system will be in use. After that time the system will not operate anymore.

Details

Preventive maintenance policies based on Warning Signal Probability criteria (WSPC) are considered. Roughly speaking, a preventive maintenance action is carried out at a time when the probability that a warning signal is received is above a prespecified value `prob`. The subset of operative states `up` is in turn split into two subsets: optimal states `up1` and operative but critical states or `up2`, where `up=up1∪up2`. Similarly, the set of green signals is split into two subsets: safe signals and warning signals. `n.green1` is the size of subset `safe`. For a given probability value (`prob`) this function first calculates the optimal inspection time

$$t.insp = \min\{t > 0 : \Pr(Y(t) \in \text{warning}, Y(u) \in \text{safe}, \forall u < t) \geq \text{prob}\}.$$

The system is inspected every `t.insp` units of time. At the time of inspection, any of three situations can be found:

1. the system is in failure, then the system is returned to operational conditions (`up1`), and a cost of `cost.C` monetary-units is implied;
2. the system is in a state of `up2`, then a preventive maintenance action is carried out, returning the system to a state in `up1` and implying a cost of `cost.P` monetary-units; and
3. the system is found in a state of `up1`, then no maintenance action is carried out and there is no associated cost.

Value

time.insp	The time at which preventive maintenance is carried out.
t.max	The maximum time that the system is being used.
n.insp	The total number of inspections that are carried out during the system lifetime, i.e. in the interval (0, t.max).
total.cost	The total cost incurred by all maintenance actions (corrective and preventive) developed in the system.

Author(s)

M.L. Gamiz, N. Limnios, and M.C. Segovia-Garcia (2024)

References

Gamiz, M.L., Limnios, N., and Segovia-Garcia, M.C. (2023). Hidden Markov models in reliability and maintenance. *European Journal of Operational Research*, 304(3), 1242-1255.

See Also

See `cost.cspc` for the implementation of the CSPC algorithm for maintenance policy.

Examples

```

model<- 'other'
rate<-p<-NA
P<-matrix(c(8,2,1,0,6,4,6,2,2)/10,3,3,byrow=TRUE)
M<-matrix(c(7,3,0,4,3,3,0,4,6)/10,3,3,byrow=TRUE)
Nx<-3; Ny<-3
n.up<-2; n.green<-2
alpha<-c(1,0,0)
hmm1<-def.hmmR(model=model,rate=NA,p=NA,alpha=alpha,P=P,M=M,Nx=Nx,Ny=Ny,n.up=n.up,n.green=n.green)
prob<-0.8;
n.up1<-n.green1<-1;cost.C<-10;cost.P<-5;t.max<-50
cost1<-cost.wcspc(prob=prob,hmmR=hmm1,n.up1=n.up1,n.green1=n.green1,
cost.C=cost.C,cost.P=cost.P,t.max=t.max)

cost1
#
v.prob<-seq(0.1,0.99,length=100)
v.cost1<-inspection.time<-double(100)
for(i in 1:100)
{cost<-cost.wcspc(prob=v.prob[i],hmmR=hmm1,n.up1=n.up1,n.green1=n.green1,
cost.C=cost.C,cost.P=cost.P,t.max=t.max)
v.cost1[i]<-cost$total.cost
#inspection.time[i]<-cost$time.insp
}
oldpar<-par(mar=c(5,5,10,10))
plot(v.prob,v.cost1,type='s',main='WSPC Algorithm for Maintenance Policy',
xlab='Probability of critical state',
ylab='Cost of maintenance')
grid()
par(oldpar)

```

 def.hmmR

Define a HMM object for Reliability Analysis.

Description

This function creates a list with all the elements that describe a HMM in the context of Reliability and Maintenance.

Usage

```
def.hmmR(model, rate, p, alpha, P, M, Nx, Ny, n.up, n.green)
```

Arguments

model	A character string to choose which HMM model is considered. Possible values are "KooN", "shock", "other"
rate	A positive real number indicating the failure rate of one unit of the system.
p	A real number in the interval (0,1) indicating the probability that the system receives one shock during a unit of time.
alpha	A vector of size Nx with the initial law of the hidden Markov chain.
P	A square matrix of dimension Nx with the transition probabilities between the hidden states.
M	A matrix of dimension Nx × Ny with the emission probabilities.
Nx	An integer indicating the total number of states in the system. By default the states are labelled: 1,...,Nx.
Ny	An integer indicating the total number of signals received. By default the signals are labelled: 1,...,Ny.
n.up	An integer lower than Nx indicating the number of (hidden) operative states in the system. The first n.up values in the state set denote operative states.
n.green	An integer lower than Ny indicating the number of signals of good performance. The first n.green signals are read as good performance of the system.

Details

- When model="KooN" the argument Nx is the maximum number of units in the system. There must be K=n.up operative units for the system to function. If K=1 a parallel system is built. If K=Nx a series system is built.
- When model="shock" the argument Nx minus 1 is the maximum number of shocks that the system can accumulate before breakdown.

Value

A list with the elements of the HMM.

states	A set of N_x characters or integers describing the hidden states of the system.
signals	A set of N_y characters or integers describing the possible signals observed.
P	A square matrix with N_x rows with the transition probabilities between the hidden states.
M	A matrix of dimension $N_x \times N_y$ with the emission probabilities.

Author(s)

M.L. Gamiz, N. Limnios, and M.C. Segovia-Garcia (2024)

References

Gamiz, M.L., Limnios, N., and Segovia-Garcia, M.C. (2023). Hidden Markov models in reliability and maintenance. *European Journal of Operational Research*, 304(3), 1242-1255.

See Also

See also `sim.hmmR` to simulate data from a given HMM.

Examples

```
## Define a HMM object describing a repairable system
## The system can be in one of 3 states: 2 up states and 1 down state.
## 3 different signals can be received: 2 good performance signals (green)
## and 1 signal of failure (red)
P<-matrix(c(8,2,1,0,6,4,6,2,2)/10,3,3,byrow=TRUE)
M<-matrix(c(7,3,0,4,3,3,0,4,6)/10,3,3,byrow=TRUE)
Nx<-3; Ny<-3
n.up<-2; n.green<-2
alpha<-c(1,0,0)
hmm1<-def.hmmR(model='other',rate=NA,p=NA,alpha=alpha,P=P,M=M,Nx=Nx,Ny=Ny,
               n.up=n.up,n.green=n.green)

hmm1
```

fit.hmmR

Non-parametric fitting of a HMM using the Baum-Welch algorithm.

Description

This function adapts the EM algorithm to fit the transition matrix of the hidden Markov chain as well as the emission probability matrix of a HMM.

Usage

```
fit.hmmR(Y,P0,M0,alpha0,max.iter=50,epsilon=1e-9,Nx,Ny)
```

Arguments

<code>Y</code>	A sequence of observations consisting of signals of system performance.
<code>P0</code>	A square matrix of dimension N_x with the transition probabilities of the hidden MC at the first iteration of the algorithm.
<code>M0</code>	A matrix of dimension $N_x \times N_y$ with the emission probabilities at the first step of the algorithm.
<code>alpha0</code>	A vector of size N_x with the initial distribution of the hidden Markov chain at the first iteration of the algorithm.
<code>max.iter</code>	An integer value with the maximum number of iterations in the iterative algorithm. Default value is <code>max.ite=50</code> .
<code>epsilon</code>	A numeric value with the tolerance in the iterative algorithm. Default value is <code>epsilon=1e-9</code> .
<code>Nx</code>	An integer value with the maximum number of states of the hidden Markov chain.
<code>Ny</code>	An integer value with the maximum number of signals emitted by the system.

Details

- The argument `alpha0` representing the initial distribution of the hidden MC is fixed, and defined by the user. The argument `Nx` is the size of the state space of the hidden MC. As default, the set of numbers $1, \dots, N_x$ is the state space of the hidden MC.
- `Ny` is the size of the alphabet of signals emitted. As default, the set of numbers $1, \dots, N_y$ is the signal-alphabet.
- The successive iterations of the algorithm can be traced and information is accessible from the outcome of this function.

Value

Among other information, this function provides the following values:

<code>P</code>	A square matrix with N_x rows with the estimated transition probabilities.
<code>M</code>	A matrix of N_x rows and N_y columns, with the estimated emission probabilities.
<code>n.iter</code>	An integer indicating the number of iterations performed in the algorithm.
<code>tol</code>	A numeric value with the achieved tolerance value in the algorithm.
<code>Fm</code>	A matrix of dimension $n \times N_x$ with the estimated forward probability values at the last iteration of the algorithm, where n is the size of the observed vector <code>Y</code> .
<code>Bm</code>	A matrix of dimension $N_x \times n$ with the estimated forward probability values at the last iteration of the algorithm.
<code>AIC</code>	The estimated value of the Akaike statistics. The number of parameters to be estimated is $nparam = N_x \cdot (N_x - 1) + N_x \cdot (N_y - 1)$.

Author(s)

M.L. Gamiz, N. Limnios, and M.C. Segovia-Garcia (2024)

References

Gamiz, M.L., Limnios, N., and Segovia-Garcia, M.C. (2023). Hidden Markov models in reliability and maintenance. *European Journal of Operational Research*, 304(3), 1242-1255.

See Also

See `def.hmmR` to define an object HMM, and `sim.hmmR` to simulate a random path from a given HMM object.

Examples

```
model<-'other'
rate<-NA
p<-NA
P<-matrix(c(0.7,0.3,1,0),2,2,byrow=TRUE)
M<-matrix(c(0.6,0.4,0,0,0,1),2,3,byrow=TRUE)
alpha<-c(1,0)
Nx<-2
Ny<-3
n.up<-1
n.green<-2
hmm0<-def.hmmR(model,rate,p,alpha,P,M,Nx,Ny,n.up,n.green)
set.seed(1969)
datos<-sim.hmmR(hmmR=hmm0,n=10)
estim<-fit.hmmR(Y=datos$Yn,P0=P,M0=M,alpha0=alpha,max.iter=50,epsilon=1e-9,Ny=3,Nx=2)
estim$P;P
estim$M;M
```

Rcalc.hmmR

Calculate the reliability of a system based on HMM.

Description

For a given time t this function returns the value of the probability that the system does not fail in the interval $(0, t]$. It gives the probability that the system survives and is still working beyond time t .

Usage

```
Rcalc.hmmR(hmmR, t)
```

Arguments

hmmR	A Hidden Markov Model.
t	A value of time, it must be an integer equal or greater than 0.

Details

The state space is split into two subsets, i.e. $states = up \cup down$. The subset up contains the states of good functioning, while the subset down contains the failure states. The signals alphabet is split into two subsets, i.e. $signals = green \cup red$. A green-signal indicates good performance of the system, while a red-signal alerts of something wrong in the system. This function returns the probability that the system has not entered the set of down states or any signal from the red subset of signals has been emitted at any time before t .

Value

This function returns the probability that the system is working through a state in the up subset, and a green signal is being received. If $t=0$, then the returned value is 1.

Author(s)

M.L. Gamiz, N. Limnios, and M.C. Segovia-Garcia (2024)

References

Gamiz, M. L., Limnios, N., and Segovia-Garcia, M.C. (2023). Hidden Markov models in reliability and maintenance. *European Journal of Operational Research*, 304(3), 1242-1255.

See Also

See `def.hmmR` to define a HMM object.

Examples

```
model<- 'other'
rate<-NA
p<-NA
P<-matrix(c(0.7,0.3,1,0),2,2,byrow=TRUE)
M<-matrix(c(0.6,0.4,0,0,0,1),2,3,byrow=TRUE)
alpha<-c(1,0)
Nx<-2
Ny<-3
n.up<-1
n.green<-2
hmm0<-def.hmmR(model=model,rate=NA,p=NA,alpha=alpha,P=P,M=M,Nx=Nx,Ny=Ny,n.up=n.up,n.green=n.green)
times<-0:30
Rt<-Rcalc.hmmR(hmmR=hmm0,t=times)
oldpar <- par(mar = c(5, 5, 10, 10))
plot(times,Rt,type='s',ylim=c(0,1),ylab='',xlab='time',main='Reliability based on HMM')
grid()
par(oldpar)
```

sim.hmmR	<i>Simulate sequence of states and signals of functioning of a system modelled by a HMM.</i>
----------	--

Description

This function simulates a sample path from a 2-dimensional HMM. It returns the hidden sequence of states and signals. At each time, the hidden state of the system is simulated from the HMM as well as the associated signal that informs on the system performance at that time.

Usage

```
sim.hmmR(hmmR, n)
```

Arguments

hmmR	A Hidden Markov Model.
n	An integer number indicating the length of the sequence of states and signals to be simulated.

Value

The function `sim.hmmR` returns a list with the following information:

Xn	The sequence of simulated hidden states.
Yn	The sequence of observed signals.
P	The transition probability matrix of the hidden Markov chain (MC).
alpha	The initial distribution of the hidden MC.
M	The emission probability matrix.
states	The set of hidden states of the system.
signal	The alphabet corresponding to the observations.

Author(s)

M.L. Gamiz, N. Limnios, and M.C. Segovia-Garcia (2024)

References

Gamiz, M.L., Limnios, N., Segovia-Garcia, M.C. (2023). Hidden Markov models in reliability and maintenance. *European Journal of Operational Research*, 304(3), 1242-1255.

See Also

See `def.hmmR` to define a HMM object.

Examples

```
## Define a HMM object describing a repairable system
P<-matrix(c(8,2,1,0,6,4,6,2,2)/10,3,3,byrow=TRUE)
M<-matrix(c(7,3,0,4,3,3,0,4,6)/10,3,3,byrow=TRUE)
hmm1<-def.hmmR(model='other',rate=NA,p=NA,alpha=c(1,0,0),P=P,M=M,Nx=3,Ny=3,n.up=2,n.green=2)
sim.hmmR(hmmR=hmm1,n=20)
```

Virkler25

Fatigue crack growth in materials: Virkler dataset (tests 1 to 25)

Description

The data consist of an aluminum alloy specimen that was tested to investigate fatigue crack propagation. Starting from an initial crack of length 9 mm for a particular item in test, the number of cycles for the size of the crack to reach a predetermined value was recorded successively. That is, it is registered the number of cycles every time an increment of size 0.2 mm in length occurs. The experiment finishes once a critical size of the crack is reached, meaning the failure of the item. The data were first published in Virkler et al. (1979) where there were 68 specimens tested to grow the initial crack of 9 mm to the final crack of 50 mm. The first 25 tests are included.

Format

A data frame with 26 variables:

- CrackLength** Length of the crack in the material.
- CycleCount1** Cycle count for the first test.
- CycleCount2** Cycle count for the second test.
- CycleCount3** Cycle count for the third test.
- CycleCount4** Cycle count for the fourth test.
- CycleCount5** Cycle count for the fifth test.
- CycleCount6** Cycle count for the sixth test.
- CycleCount7** Cycle count for the seventh test.
- CycleCount8** Cycle count for the eighth test.
- CycleCount9** Cycle count for the ninth test.
- CycleCount10** Cycle count for the tenth test.
- CycleCount11** Cycle count for the eleventh test.
- CycleCount12** Cycle count for the twelfth test.
- CycleCount13** Cycle count for the thirteenth test.
- CycleCount14** Cycle count for the fourteenth test.
- CycleCount15** Cycle count for the fifteenth test.
- CycleCount16** Cycle count for the sixteenth test.
- CycleCount17** Cycle count for the seventeenth test.

CycleCount18 Cycle count for the eighteenth test.
CycleCount19 Cycle count for the nineteenth test.
CycleCount20 Cycle count for the twentieth test.
CycleCount21 Cycle count for the twenty-first test.
CycleCount22 Cycle count for the twenty-second test.
CycleCount23 Cycle count for the twenty-third test.
CycleCount24 Cycle count for the twenty-fourth test.
CycleCount25 Cycle count for the twenty-fifth test.

References

Virkler, D. A., Hillberry, B. M., and Goel, P. K. (1979). The statistical nature of fatigue crack propagation. *Journal of Engineering Materials and Technology*, 101 , 148–153 .

Examples

```
data(Virkler25)
i<-1 ## choose specimen number 1
ti<-Virkler25[(i+1)]/10000 ## cycles at which the cracksize increases 0.2 units.
yt<-Virkler25[,1] ##
### the system is observed every 2000 cycles (0.2 unit times)
### observations:
t.obs<-seq(0,max(ti),by=0.2)
yi<-approx(x=ti,y=yt,xout=t.obs,method='linear',rule=2)$y
yi<-diff(yi)
#discretize the observations:
yi<-kmeans(yi,4)$cluster ## consider an alphabet of 4 signals
Nx<-2; # consider 2 hidden states
Ny<-4
alpha0<-c(1,0)
estim<-fit.hmmR(Y=yi,P0=NA,M0=NA,alpha0=alpha0,max.iter=50,epsilon=1e-9,Nx=Nx,Ny=Ny)
estim$P
estim$M
```

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